

CHAIN RULE DIAGRAMS

Construct a tree diagram and a chain rule formula for each of the indicated derivatives.

1. $z = f(x, y), x = x(u, v), y = y(u, v), \frac{\partial z}{\partial u} = ?$

2. $z = f(x, y), x = x(u, v), y = y(u, v), u = u(s, t), v = v(s, t), \frac{\partial z}{\partial s} = ?$

3. $z = f(x, y), x = x(t), y = y(t), \frac{dz}{dt} = ?$

4. $z = f(x, y), x = x(s), y = y(t), \frac{\partial z}{\partial t} = ?$

5. $w = f(x, y, z), x = x(t, u, v), y = y(t, u, v), z = z(t, u, v), \frac{\partial w}{\partial t} = ?$

6. $w = f(x, y, z), x = x(u, v), y = y(u, v), z = z(u, v), u = u(s), v = v(t), \frac{\partial w}{\partial t} = ?$

7. $w = f(x, y, z), x = x(u, v), y = y(u, v), z = z(u, v), u = u(t), v = v(t), \frac{dw}{dt} = ?$

8. $w = f(x, y, z), x = x(u, v), y = y(u, v), z = z(u, v), \frac{\partial w}{\partial v} = ?$