

LIMITS

Either find the indicated limit, or show that the limit fails to exist by evaluating it along two different paths and arriving at two different results.

$$1. \lim_{(x,y) \rightarrow (0,0)} \cos(xy)$$

$$2. \lim_{(x,y) \rightarrow (0,0)} e^{xy}$$

$$3. \lim_{(x,y) \rightarrow (0,0)} \frac{3x^2 - 2y^2}{x^2 + y^2}$$

$$4. \lim_{(x,y) \rightarrow (1,-1)} \frac{x^2 - 2xy + y^2}{x - y}$$

$$5. \lim_{(x,y) \rightarrow (0,0)} \frac{x^2 - 2xy + y^2}{x - y}$$

$$6. \lim_{(x,y) \rightarrow (1,1)} \frac{x^2 - y^2}{x - y}$$

$$7. \lim_{(x,y) \rightarrow (0,0)} \frac{x}{y}$$

$$8. \lim_{(x,y) \rightarrow (0,0)} \frac{x^4 y^2}{x^8 + y^4}$$