POSITION, VELOCITY, AND ACCELERATION

Find the position and velocity functions having the given acceleration and initial position and velocity at time t = 0 seconds. Then find the speed at time t = 5 seconds. Assume that the units associated with distance are feet.

1.
$$\vec{a}(t) = -32\hat{k}, \ \vec{v}(0) = \vec{0}, \ \vec{r}(0) = 100\hat{k}$$

2.
$$\vec{a}(t) = -32\hat{k}, \ \vec{v}(0) = -3\hat{k}, \ \vec{r}(0) = 100\hat{k}$$

3.
$$\vec{a}(t) = -32\hat{k}, \ \vec{v}(0) = 10\hat{i} + 10\hat{j} + 10\hat{k}, \ \vec{r}(0) = \vec{0}$$

4.
$$\vec{a}(t) = -\cos(t)\hat{i} - \sin(t)\hat{j}, \ \vec{v}(0) = -\hat{i}, \ \vec{r}(0) = \hat{j}$$

5.
$$\vec{a}(t) = -5\cos(t)\hat{i} - 5\sin(t)\hat{j}, \ \vec{v}(0) = -5\hat{i} + 5\hat{j}, \ \vec{r}(0) = 5\hat{i} + 5\hat{j}$$